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Numerical Aspects of the ICON Atmosphere Model

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Outline

The ICON modelling framework model components, historical review

Model Grid

horizontal and vertical grid topology

Governing equations and discretization aspects

prognostic variables, temporal and spatial discretization

Physics-dynamics coupling coupling strategy, NWP physics package

Diffusion and Filters

divergence averaging, IAU, sponge layers, hyperdiffusion

Progress in Forecast Quality past decades until today





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The ICON Modelling Framework

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ICON component models

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Flavors of ICON-Atmosphere

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- Identical dynamical core + tracer transport \succ (nonhydrostatic core is able to handle all scales)
- Differences wrt the physical parameterization suite \geq



Different grid resolutions require different level of parameterization



A brief historical account of ICON (NWP)

- Decision about cooperation between DWD und MPI-M for a joint 2001 development of a new global modelling system for NWP and climate
- First project positions; development of a shallow-water model based on the 2004 ICON grid structure
- Hydrostatic dynamical core with numerics partly imported from ECHAM, 2008 start of implementation of tracer transport schemes.
- Nonhydrostatic dynamical core, coupling with physics parameterizations. 2010
- First real-data tests 2011
- First **comparison** of forecast skills **against GME** based on IFS analyses 2012 (encompassed by extensive test series in order to optimize forecast quality)







A brief historical account of ICON (NWP)

- **Coupling to 3D-Var** data assimilation scheme. Further experiments to 2012 optimize forecast quality.
- 08 / 2014 Start of preoperational phase
- 01 / 2015 Start of operational production at DWD (13 km, 90 levels up to 75 km)
- **06 / 2015** Activation of **nested domain over Europe** (6.5 km, 60 levels up to 22.5 km)
- **Ensemble data assimilation system** (Localized Ensemble Transform 01 / 2016 Kalman Filter, 40 members)
- Start of operational production for regional mode ICON-D2 (2.2 km, 60 02 / 2021 levels up to 22.5 km, 40 members)
- 07 / 2024 operational rapid update cycle ICON-D2-RUC













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Horizontal grid topology

- > grid generation is based on the Icosahedron
- > By RnBk we denote a grid that originates from an icosahedron whose
 - edges have been initially divided into n parts,
 - followed by k subsequent edge bisections.
 - grid optimized by 'spring dynamics' step
- > The total number of grid cells in the ICON grid is given by

 $n_{\rm cells} = 20 \, \mathbf{n}^2 4^{\mathbf{k}}$

> Operationally used at DWD: R3B7 ≈ 2.95 million cells





Comparison to regular lat-lon

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Planar torus grid



- > It is possible to run ICON on a planar torus grid
- > Equilateral planar triangles, doubly-periodic



Useful for

- idealized LES applications (e.g. convective/neutral/stable PBL)
- quasi 2D (x-z) idealized simulations (e.g. "Straka" test)



 $\Delta x = \Delta z = 25n$ 300 5 4.0 298.5 296.5 3.0 [w] z 2.0 294.5 292 5 290.5 288 5 286.5 1.0 284.5 282.5 27.0 30.0 33.0 36.0 39.0 42.0 x [km]

"Straka" density current test



Theta

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more rapid decay of small scale features

Vertical coordinate system

terrain features decay linearly with height

- **Terrain following, time constant, hybrid σ-z coordinates** (i.e. height based !) \succ
- Level ordering: top-down \succ
- Constructed during setup phase on the basis of namelist settings (sleve nml) \geq i.e. no input fields required





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Prognostic variables and staggering

- > Arakawa C-staggering in the horizontal
- Lorenz-type staggering in the vertical
- Top-down numbering



3D grid: prismatic cells







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Governing Equations and Discretization Aspects

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Full set of governing equations

- > Navier-Stokes fully compressible, Hesselberg averaged, rotating reference frame
 - spherical geoid
 - shallow atmosphere (optional: deep atmosphere)
- \succ vector invariant form $(\boldsymbol{u}\cdot\nabla\boldsymbol{u}=\nabla K+\boldsymbol{\zeta} imes \boldsymbol{u})$



prognostic

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Tutorial

Sec 3.1

dry air

- Equation set describes two-component (dry air + water) multiphase flow
 derivation requires choice of a reference velocity
- Formulated in a barycentric reference frame (Wacker et. al, 2003)

 → reference frame impacts the specific form of the equation set
- Reference velocity (prognostic!) is the barycentric velocity rather than the dry air velocity

$$oldsymbol{v}_{bc} = rac{\sum_k
ho_k oldsymbol{v}_k}{\sum_k
ho_k}$$





Current implementation of the barycentric system uses an **approximate lower boundary condition**,

i.e. $w_{bc} = 0$ at the surface



"Dynamical core" versus "Physics"

Dynamical core: the resolved fluid component of the model

((non)-linear transport terms, pressure gradient, numerical filters)

Physics: sub-grid scale processes

(microphysics, radiation, turbulence ...)

Numerical filters and diffusion $\frac{\partial \widehat{v}_n}{\partial t} + \frac{\partial K_h}{\partial n} + (\widehat{\zeta} + f)\widehat{v}_t + \widehat{w}\frac{\partial \widehat{v}_n}{\partial z} + c_{pd}\widehat{\theta}_v\frac{\partial \pi'}{\partial n} + F_{v_n} = -\frac{1}{\overline{a}}\left(\nabla_h \cdot \overline{\rho v''v''}\right) \cdot e_n$ $\frac{\partial \widehat{w}}{\partial t} + \widehat{v}_h \cdot \nabla \widehat{w} + \widehat{w} \frac{\partial \widehat{w}}{\partial z} + c_{pd} \left(\widehat{\theta}_v \frac{\partial \pi'}{\partial z} + \theta'_v \frac{\mathrm{d}\pi_0}{\mathrm{d}z} \right) + F_w = -\frac{1}{\overline{\rho}} \frac{\partial}{\partial z} \overline{\rho v'' v''}$ $\frac{c_{vd}c_{pd}}{R_d}\overline{\rho}\widehat{\theta}_v\frac{\partial\overline{\pi}}{\partial t} + c_{pd}\overline{\pi}\,\nabla\cdot\left(\overline{\rho}\widehat{\boldsymbol{v}}\widehat{\theta}_v\right) - c_{pd}\overline{\pi}\,\overline{\rho}\widehat{\theta}_v\chi\nabla\cdot\widehat{\boldsymbol{v}} + F_{\pi} = c_{pd}\overline{\pi}\,\overline{\rho}\overline{Q}$ $\frac{\partial \overline{\rho}}{\partial t} + \nabla \cdot (\overline{\rho} \widehat{\boldsymbol{v}}) = 0$ $\frac{\partial \overline{\rho} \widehat{q}_k}{\partial t} + \nabla \cdot \left(\overline{\rho} \widehat{q}_k \widehat{\boldsymbol{v}} \right) = -\nabla \cdot \left(\overline{J}_k^z \boldsymbol{k} + \overline{\rho} \overline{q}_k'' \boldsymbol{v''} \right) + \overline{\sigma}_k$



Numerical discretization: general remarks

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Focus on computational speed/scalability rather than ultra high convergence rates

- Avoidance of implicit methods no global communication
- Fully explicit time integration scheme Exception: terms describing vertical sound wave propagation
- Mixture of finite volume/finite difference discretization methods mostly of 2nd order in space and time
- Local methods with small stencils only direct neighbors and vertex-neighbors







For details see Zängl et al. (2015)



The time integration scheme in a nutshell

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- > Explicit two-time-level predictor-corrector time stepping scheme for v_n , w, ρ , π
- > All terms integrated at the acoustic time step (not split-explicit)
- > Exception: **implicit treatment** of terms describing **vertical sound wave** propagation (w_z , π_z). Involves solution of linear tridiagonal system for w in the vertical column.

Predictor-Corrector basic principle

Let

$$\frac{\partial \phi}{\partial t} = F(\phi, t), \text{ with } \phi \in v_n, w, \rho, \pi$$

predictor

r
$$\phi^{(n+1)*} = \phi^n + \Delta t F(\phi^n)$$

corrector

$$\phi^{n+1} = \phi^n + \Delta t \left(\alpha F(\phi^n) + \beta F(\phi^{(n+1)*}) \right); \quad \alpha + \beta = 1$$



Tutorial Sec 3.5

Time-splitting

- > Time-splitting between the dynamical core and tracer advection/physics
- > Dynamical core is sub-cycled wrt. tracer advection and physics







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Physics-Dynamics coupling

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- We distinguish between "fast physics" and "slow physics"
- On the basis of process time scales versus model time step
- Processes are treated isochorically (ρ=const, not p!)





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Physics-Dynamics coupling

- We distinguish between "fast physics" and "slow physics"
- On the basis of process time scales versus model time step
- Processes are treated isochorically (ρ=const, not p!)

Fast physics

- called every advection time step (dtime)
- treated in sequential-update split mode
 - model state is updated after each process





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Physics-Dynamics coupling

- We distinguish between "fast physics" and "slow physics"
- On the basis of process time scales versus model time step
- Processes are treated isochorically (ρ=const, not p!)

Slow physics

- Called every kth fast physics time step (k ≥ 1 is process dependent)
- treated in parallel-split split mode
 - all processes are computed from the same model state
- tendencies are passed to the dynamical core





The NWP physics package

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Process		Scheme	Settings	
Radiation		RRTM Not recommended Mlawer et al. (1997), Barker et al. (2003)	inwp_radiation=1	
	Ø	ecRad Hogan and Bozzo (2018)	inwp_radiation=4	(We 09:45)
Non-orographic gravity wave drag	Ø	Wave dissipation at critical level Orr et al. (2010)	inwp_gwd=1	
Sub-grid scale orographic drag	Ø	Lott and Miller scheme Lott and Miller (1997)	inwp_sso=1	
Microphysics	M	Single-moment scheme Doms et al. (2011), Seifert (2008)	inwp_gscp=1, 2	(We 14:00)
		Double-moment scheme Seifert and Beheng (2006)	inwp_gscp=4	فسربوس
new		Mixed-phase Spectral Bin Microphysics (SBM) Khain and Sednev (1996), Khain et al. (2004)	inwp_gscp=8	

nwp_phy_nml



The NWP physics package

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Process		Scheme	Settings	
Convection		Mass-flux shallow and deep	inwp_convection=1	
		Tiedtke (1989), Bechtold et al. (2008)		
Cloud cover		Diagnostic PDF	inwp_cldcover=1	
		M. Köhler et al. (DWD)		
		All-or-nothing scheme (grid-scale clouds)	inwp_cldcover=5	
Turbulent diffusion		Prognostic TKE (COSMO)	inwp_turb=1	We 11:45
		Raschendorfer (2001)		Lunn M
		3D Smagorinsky diffusion (for LES)	inwp_turb=5	
		Smagorinsky (1963), Lilly (1962)		
Land	Ø	Tiled TERRA	inwp_surface=1	(mm)
		Schrodin and Heise (2001), Schulz et al. (2016)		(We 11:00 کی ک
		Flake: Mironov (2008)	llake=.TRUE.	
		Sea-ice: Mironov et al. (2012)	lseaice=.TRUE.	J



nwp_phy_nml

The NWP physics package

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Process	Scheme	Settings
Convection	Mass-flux shallow and deep Tiedtke (1989), Bechtold et al. (2008)	inwp_convection=1 We 14:0
Cloud cover	Diagnostic PDF <i>M. Köhler et al. (DWD)</i>	inwp_cldcover=1
	All-or-nothing scheme (grid-scale clouds)	inwp_cldcover=5
Turbulent diffusion	Prognostic TKE (COSMO)	inwp_turb=1

Warning!

Do not patch together randomly! Not all combinations are tested or even foreseen. The model may crash without throwing a proper error message.

	Schrodin and	Heise (2001), Schulz et al. (2016)		(We 11:00)
	Flake: Miron	ov (2008)	llake=.TRUE.	
nwp_phy_nml	Sea-ice: Mirc	onov et al. (2012)	lseaice=.TRUE.	



Reduced radiation grid

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Hierarchical structure of the triangular mesh is suitable for calculating physical processes (e.g. radiative transfer) with different spatial resolution compared to dynamics.







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Numerical Aspects of the ICON Atmosphere Model



- All numerical models need some form of dissipation (either explicitly, or inherent in the numerical schemes)
- Dissipation may serve many purposes
 - removing numerical noise (due to dispersion errors, computational modes, initialization, grid-scale forcing from physics)
 - prevent the accumulation of energy at the grid scale
 - numerical stabilization
- Explicit diffusion/filters:

extra terms (non-physical) added to the discrete momentum and thermodynamic equations

$$\frac{\partial \psi}{\partial t} = \text{Dyn}(\Psi) + \text{Phys}(\Psi) + \mathbf{F}_{\Psi} \qquad \Psi = v_n, w, \theta_v, q_k$$



Checkerboard noise on triangular C-grids

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- Triangular C-grid suffers from spurious computational mode (e.g. Danilov (2010)), triggered by the discrete divergence operator (Wan et al. (2013))
- > Divergence operator in ICON: applies the Gauss theorem



$$\operatorname{div}\left(\mathbf{v}\right) = \frac{1}{A_{i}} \sum_{e=1}^{3} v_{n,e} \left(\mathbf{N}_{e} \cdot \mathbf{n}_{i,e}\right) \, l_{e}$$

Truncation error analysis:

div
$$(\mathbf{v}) = \overline{(\nabla \cdot \mathbf{v})} + (-1)^{\delta} l H(\mathbf{v})_0 + \mathcal{O}(l^2)$$

- > Operator only 1st order accurate on triangular C-grid
- Error changes sign from upward- to downward pointing triangle => checkerboard



Example: Jablonowski baroclinic wave test

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Standard divergence operator







Pragmatic solution: velocity averaging



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5-point velocity averaging



div
$$(\mathbf{v}) = \frac{1}{A_i} \sum_{e=1}^{3} \mathbf{v}_{n,e} \mathbf{N}_e \cdot \mathbf{n}_{i,e} l_e$$



- \geq Achieves (almost) second-order accurate divergence operator
- Loosely termed divergence averaging \geq (even though it is the velocity which is averaged)
- \geq unconditionally activated in the dynamical core

For details see Zängl et al. (2015)





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Problem

- > Analysis fields (best guess of the atm. state) are not perfectly balanced.
- Leads to the generation of spurious sound and gravity waves in forecast runs.
- Decay timescale ≈ 1d (R3B7)
- Consequences:
 - accumulation of noise in the assimilation cycle
 - spin-up effects in forecast runs
- > Filtering of initial conditions required





Solution

- > IAU: Filtering procedure during model initialization
- Widely used at operational NWP centers
- Strategy:
 - analysis increments (FG ANA) are added incrementally over many timesteps
 - filters small scale non-balanced modes (low pass filter)



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- IAU effectively damps small scale noise (blue)
- DWD product "initialized analysis" (= filtered analysis) (green)
- Recommended dataset for initializing standalone forecast runs (without data assimilation cycle)
- Noise level during spinup phase is somewhat larger than with full IAU cycle, but much smaller than when skipping IAU at all.
- initialized analysis available via the PAMORE web service for deterministic runs (see talk by Daniel Rieger).





Additional filtering mechanisms in ICON



higher order (q>1) improves scale selectivity

```
hdiff_order
lhdiff_{temp,vn,w,q}
hdiff_xyz
(diffusion_nml)
```

2D/3D divergence damping

- diffusion of the divergent part of the flow
- 2D: reduces high-frequency gravity wave noise
- 3D: acoustic mode filtering

divdamp_type
divdamp_order
damp_xyz
(nonhydrostatic_nml)



for momentum and thermodynamic eqs.



for momentum eq.

For details see Zängl et al. (2015)



Additional filtering mechanisms in ICON



Sponge layer at model top

- minimize spurious wave reflections at (rigid) model top by absorbing most of the incoming energy
- acts by damping vertical velocity

rayleigh_type
rayleigh_coeff
damp_height
(nonhydrostatic_nml)







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NWP forecast quality over time (1968-2024)

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Progress in forecast quality (2020-2025)

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WMO verification against radiosondes level: **500hPa**

lead-time: +48h

valid-time: 12UTC

score: rmse



France Canada U-Kingdom ECMWF DWD



Thanks to Felix Fundel (DWD)

Progress in forecast quality (2020-2025)

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Date



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Thank you for your attention



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> For most NWP applications a **vertically stretched grid** is used.

- > Layer thickness increases with height.
- Very small vertical aspect ratio \Delta z/\Delta x << 1</p>
- > Pancake-like prismatic cells



... compared to previous global and regional NWP models at DWD

- Better conservation properties (local mass conservation)
 - flux form for prognostic quantities ρ and q_k
- Mass consistent tracer transport (tracer air-mass consistency)
- > Applicability on a wide range of scales from ~100 km to ~100 m
 - fully compressible (nonhydrostatic) equation set
- Scalability and efficiency on massively parallel computer architectures with O(10⁴ +) cores
 - Fully explicit, local numerical methods
- Possibility of static mesh refinement/nesting (see upcoming talk)
- > ... and much **better quality** of operational weather forecasts

